

# A Global Fit of EW data incl. $b \rightarrow s\gamma$ , $a_\mu$ and Higgs limits in the SM and CMSSM

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## Outline

- Comparison of SM and CMSSM global fits
- $g-2$  constraints
- $b \rightarrow s\gamma$  in NLO
- Higgs masses

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<sup>a</sup>Talk at: <http://home.cern.ch/~deboerw>

# MSSM-FITTER vs SM

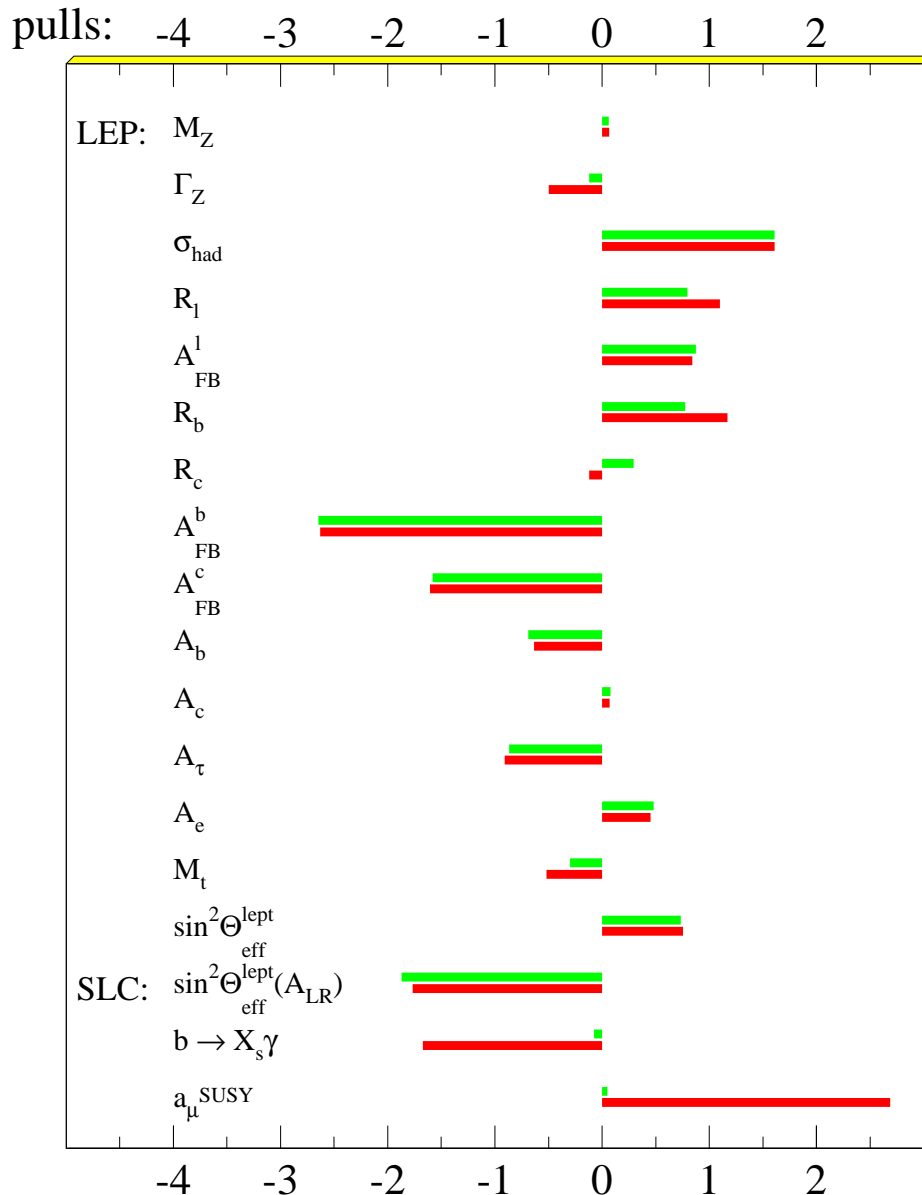
Fit results in SM and MSSM!! (Data 2001)  
MSSM better  $\chi^2$  because of  $a_\mu^{SUSY}$  and  $b \rightarrow X_s \gamma$

Data / SM

$\chi^2/\text{d.o.f} = 34.0/18$

Data / MSSM ( $\tan\beta = 35$ )

$\chi^2/\text{d.o.f} = 25.0/13$



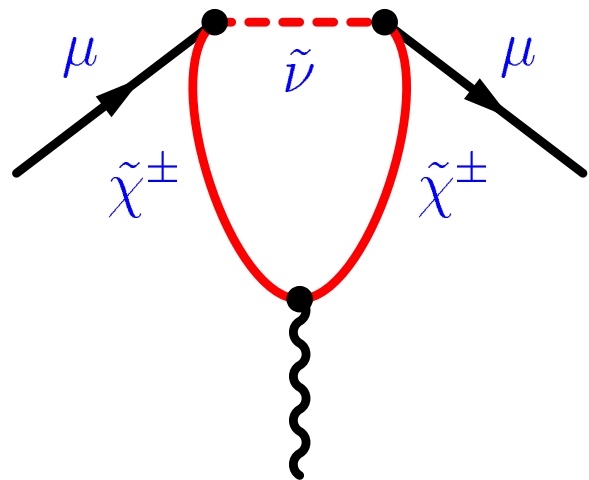
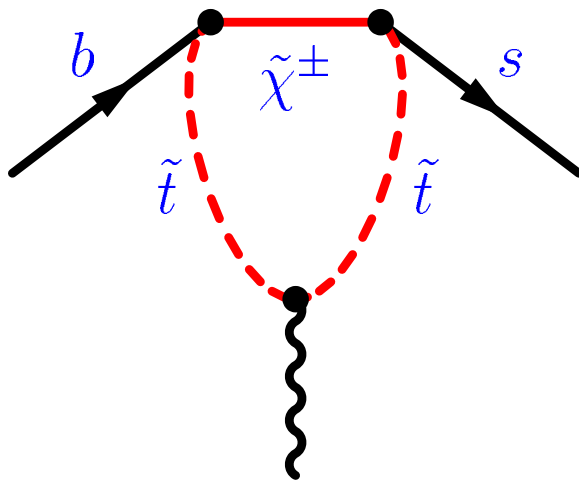
MSSM results from MSSM-Fitter (see WdB, W. Hollik et al.,  
Z.Phys. C75(1997) 627 and hep-ph/9609209)

SM results obtained with ZFITTER6.11 (see D. Bardin et al.,  
hep-ph/9412201)

# Main SUSY contr. to $b \rightarrow X_s \gamma$ and $a_\mu$

$b \rightarrow s \gamma$

muon anom. magnetic moment



## Best Fitted SUSY masses $\tan \beta=35$

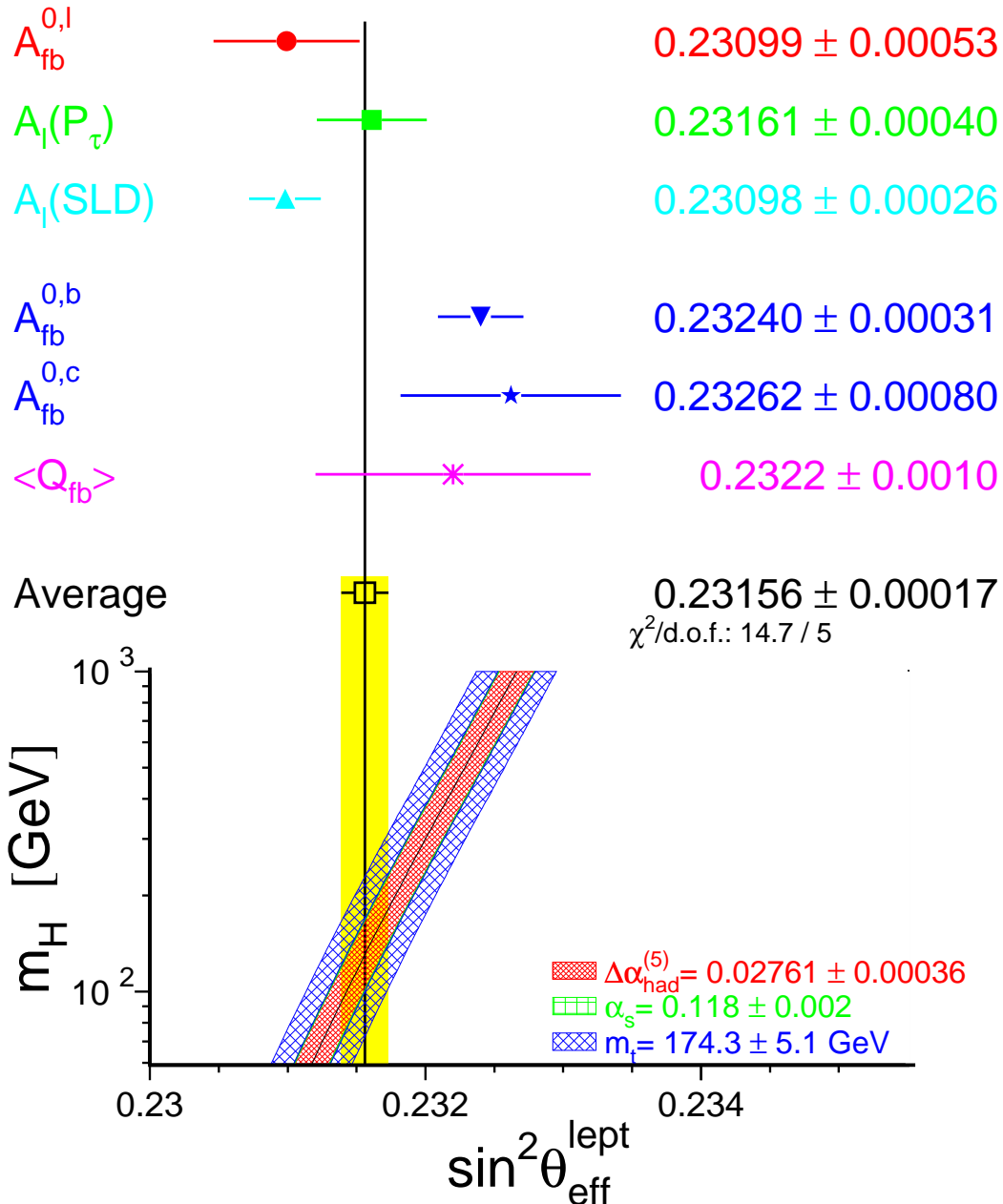
| Symbol                   | [GeV] | Symbol                 | [GeV] |
|--------------------------|-------|------------------------|-------|
| $m_{\tilde{\chi}_1^\pm}$ | 105   | $m_{\tilde{\chi}_1^0}$ | 66    |
| $m_{\tilde{\chi}_2^\pm}$ | 217   | $m_{\tilde{\chi}_2^0}$ | 110   |
| $m_{\tilde{t}_1}$        | 600   | $m_{\tilde{\chi}_3^0}$ | 156   |
| $m_{\tilde{t}_2}$        | 710   | $m_{\tilde{\chi}_4^0}$ | 216   |
| $m_{\tilde{\nu}}$        | 500   |                        |       |

**EW FIT: NO common GUT scale parameters assumed for sleptons and squarks**

$a_\mu$  wants charginos close to experimental limit  
 Sleptons and squarks at intermediate masses, else ew precision data changed.

# Summary of $\sin^2 \Theta_W^{eff}$

Preliminary

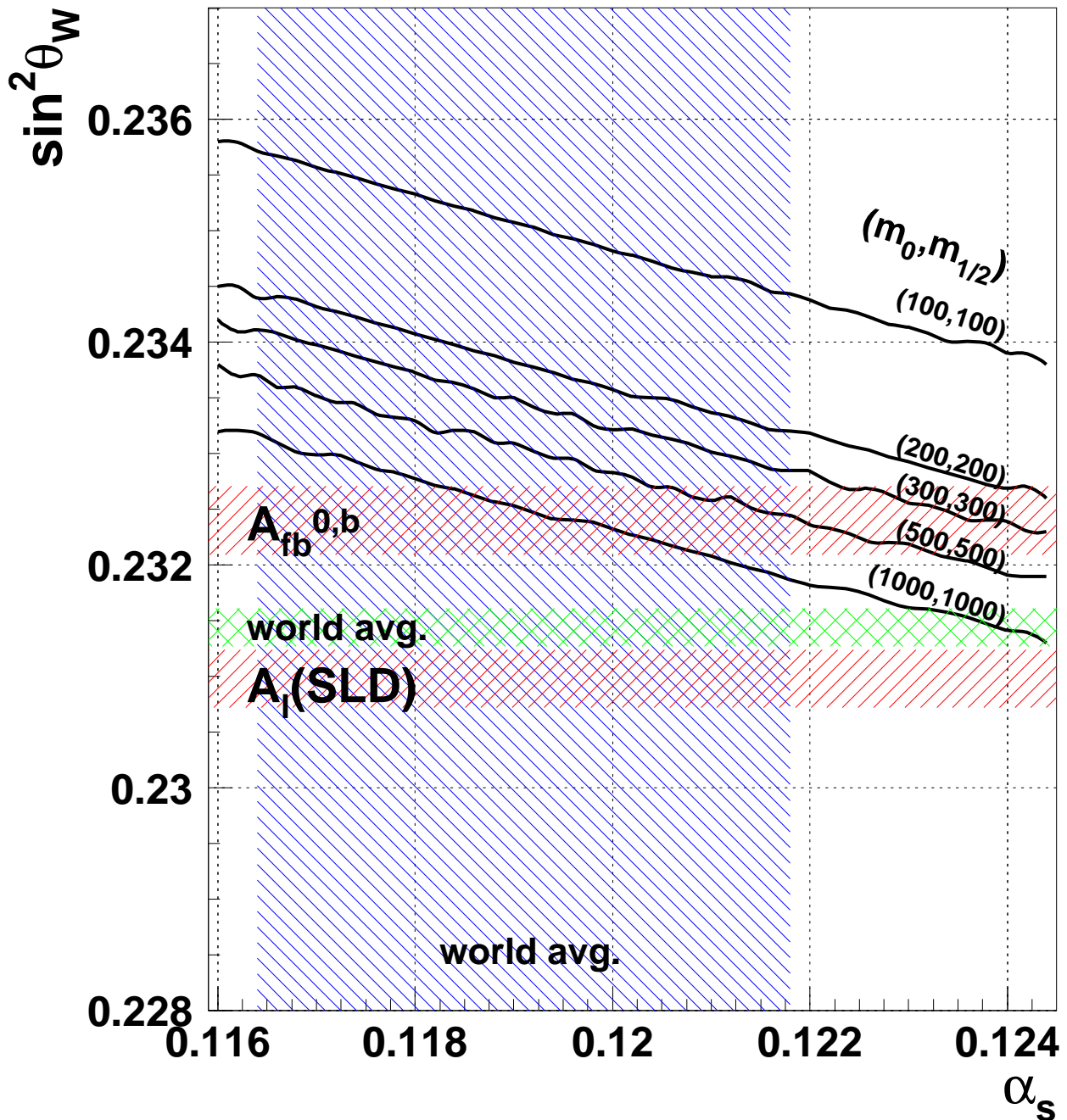


**Most sensitive  $\sin^2 \theta_W^{eff}$  values more than  $3\sigma$  apart!!**  
**Averaged value independent of Higgs constraint in the fit!!!**

**Higgs mass =  $F(M_t, \alpha, \sin^2 \theta_W)$**

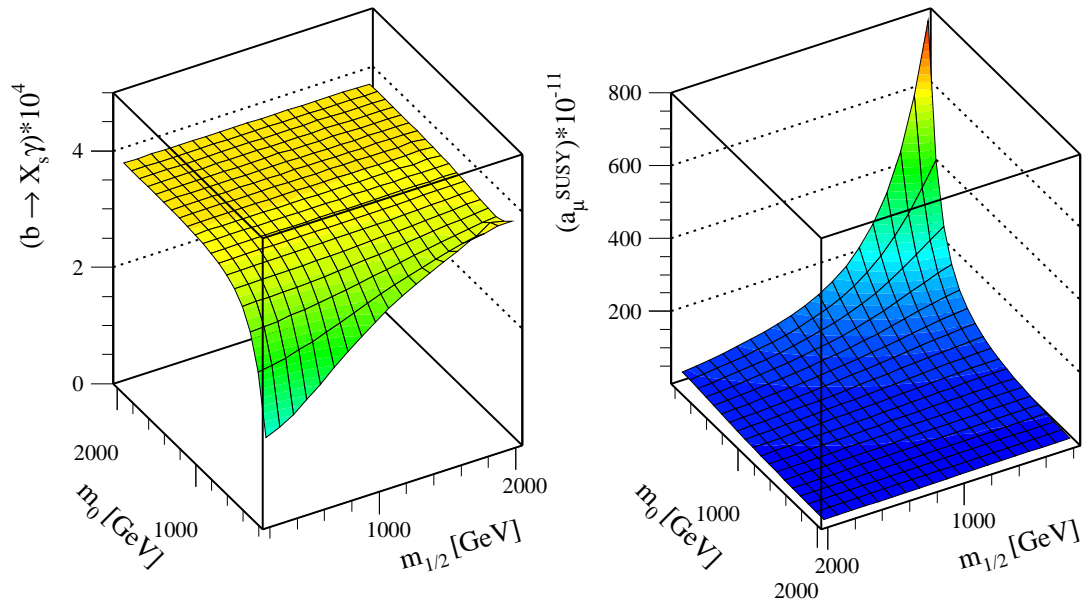
**Requiring  $m_h > 113.5$  increases  $M_t$  from fit by 1.1 GeV and reduces  $\alpha$  a little, but errors on  $\sin^2 \theta_W$  so small compared with error on  $M_t$ , that couplings are not changed by Higgs constraint.**

# Which CC needed for unification?



Most precise  $\alpha_s$  values (calc. up to  $\mathcal{O}(\alpha_s^3)$ ):  
 $\alpha_s$  from  $R_l = 0.1231 \pm 0.0037^{+0.0033}_{-0.0000}$  (Higgs)  
 $\alpha_s$  from  $\sigma_{tot} = 0.1159 \pm 0.0041^{+0.0026}_{-0.0000}$  (Higgs)  
 ( $\sigma_{tot}$  dominated by theoretical error on luminosity!!)

# $\text{Br}(b \rightarrow X_s \gamma)$ and $a_\mu^{\text{SUSY}}$



## • New measurements:

CLEO (F. Blanc, Moriond, 2001 and hep-ex/9908022):

$$\text{BR}(b \rightarrow s \gamma) = (2.85 \pm 0.35_{\text{stat}} \pm 0.22_{\text{sys}}) \cdot 10^{-4}$$

ALEPH (PL B429 (1998) 169):

$$\text{BR}(b \rightarrow s \gamma) = (3.11 \pm 0.80_{\text{stat}} \pm 0.72_{\text{sys}}) \cdot 10^{-4}$$

BELLE (hep-ex/0103042, Phys. Lett. B511 (2001) 151):

$$\text{BR}(b \rightarrow s \gamma) = (3.36 \pm 0.53_{\text{stat}} \pm 0.42_{\text{sys}} \pm 0.50_{-0.54}^{\text{(model)}}) \cdot 10^{-4}$$

Weighted Average:

$$\text{Br}(b \rightarrow X_s \gamma) = 2.96 \pm 0.35 \cdot 10^{-4}$$

- $m_c/m_b = 0.29$  for pole masses.

Should one use running mass for charm quark in loop:

$$m_c(\mu)/m_b = 0.22 ??$$

(Gambino and Misiak, hep-ph/0104034)

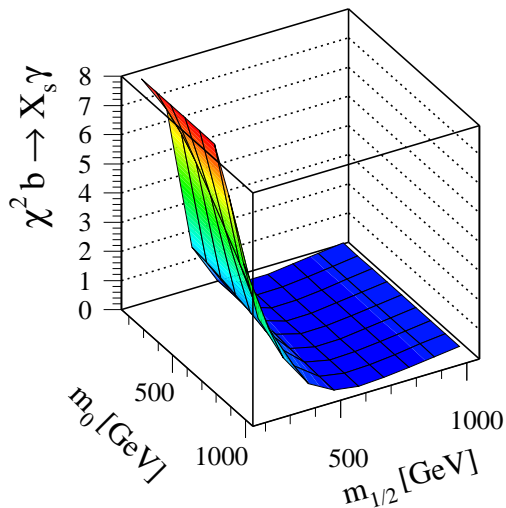
Increases SM prediction for  $\text{Br}(b \rightarrow X_s \gamma)$  by  $\mathcal{O}(10\%)$

$$\text{Br}(b \rightarrow X_s \gamma) = (3.73 \pm 0.3) \cdot 10^{-4} \text{ in the SM.}$$

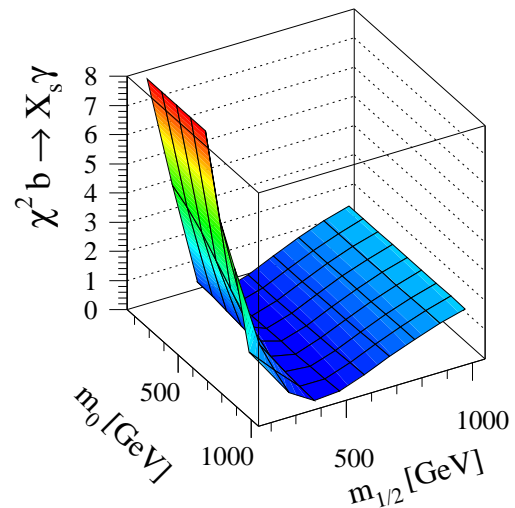
**Data now  $1.7\sigma$  below SM prediction?**

# $\text{Br}(b \rightarrow X_s \gamma)$ and $a_\mu^{\text{SUSY}}$

Old

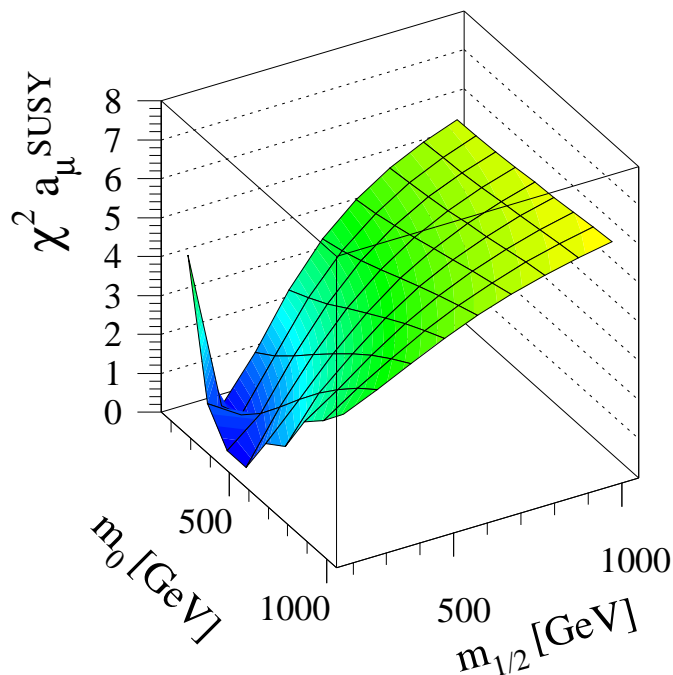


New



“Old”  $b \rightarrow X_s \gamma$  with  $m_c/m_b = 0.29$  wants heavy sparticles

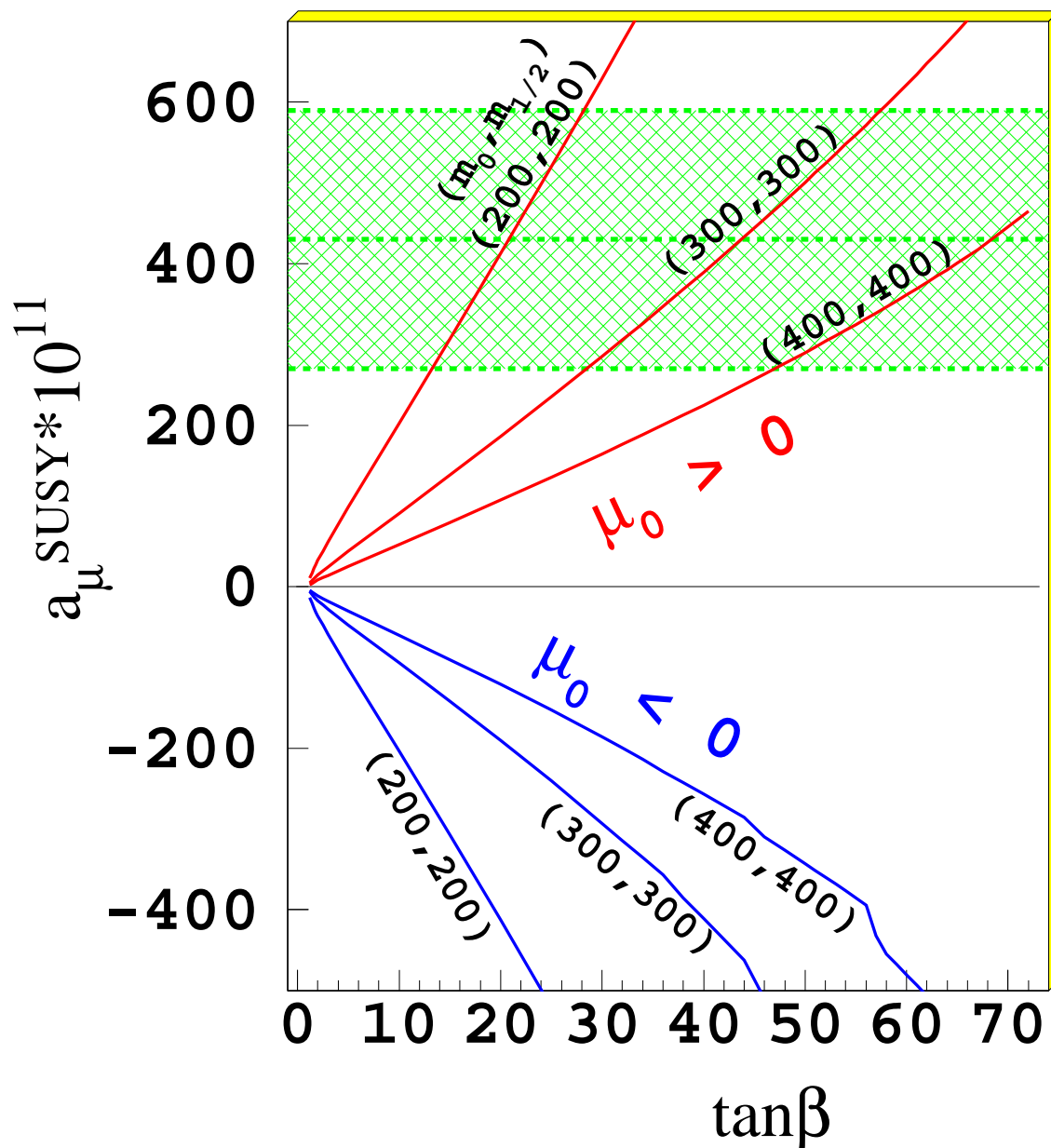
“new”  $m_c/m_b = 0.22$  with current c-quark mass wants intermediate sparticles



$a_\mu^{\text{SUSY}} = 425 \cdot 10^{-11}$  wants light sparticles

# Anom. magn. moment $a_{\mu}^{SUSY}$ vs $\tan \beta$

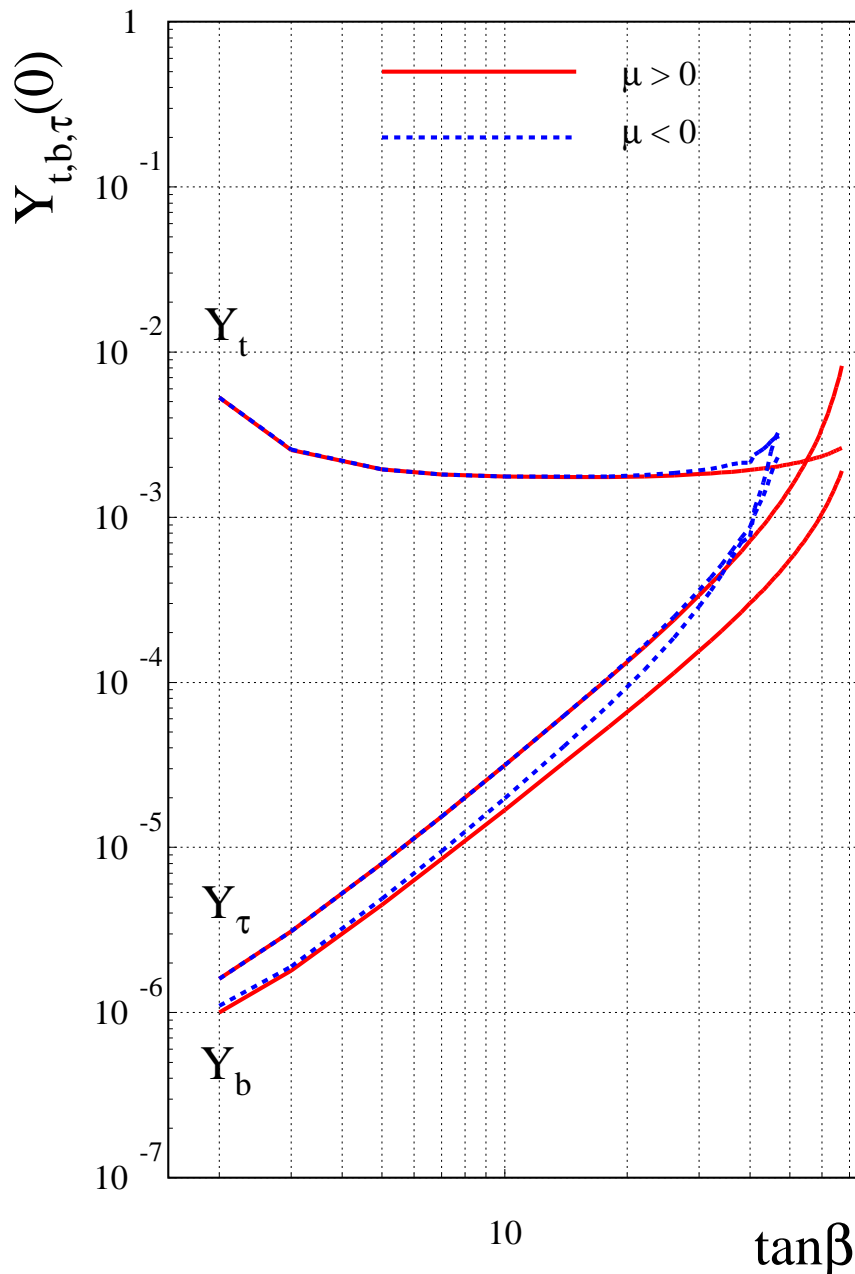
SUSY contributes via chargino-sneutrino or neutralino-smuon loops



- $a_{\mu}^{SUSY} \propto \tan \beta$  (Czarnecki, Marciano, Nath, ..)
- $\mu < 0$  excluded
- GUT scale mass parameters required to be in 100-500 GeV range

# Yukawa Couplings vs. $\tan \beta$

Determine Yukawa's at GUT scale from  $m_t$ ,  $m_b$  and  $m_\tau$  by running RGE! Result insensitive to  $m_0, m_{1/2}$ .



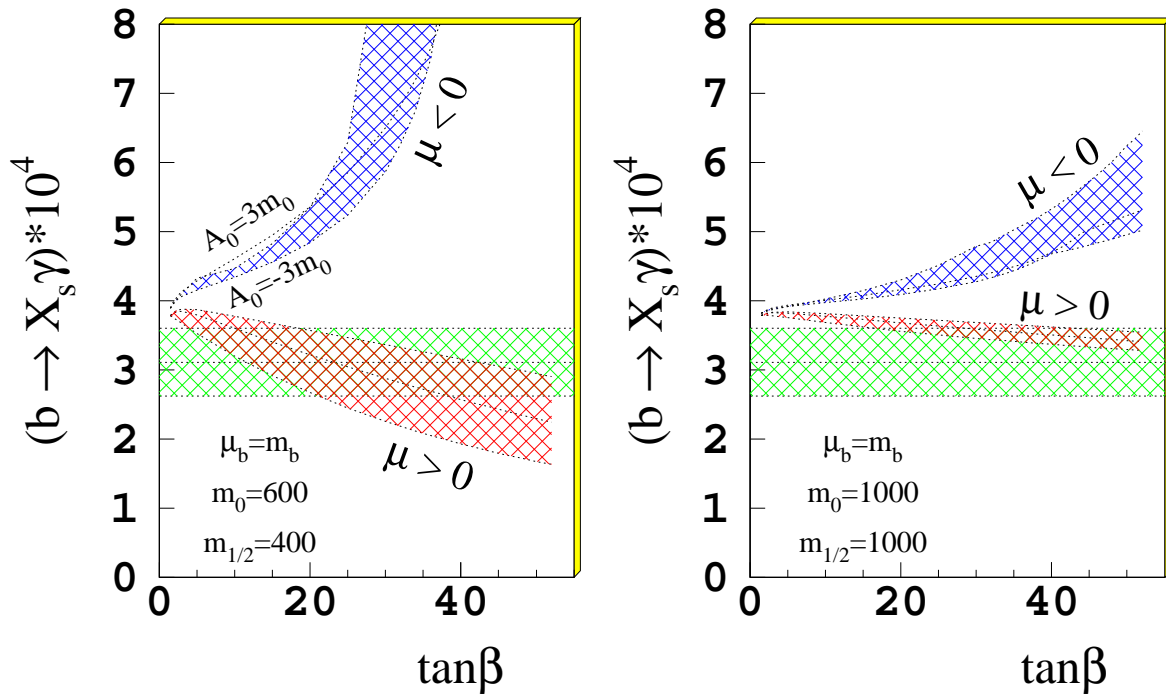
$$m_t^2 = (4\pi v)^2 Y_t \frac{\tan \beta^2}{1 + \tan \beta^2} m_{b(\tau)}^2 = (4\pi v)^2 Y_{b(\tau)} \frac{1}{1 + \tan \beta^2}$$

**Triple Unification at  $\tan \beta \approx 45$  for  $\mu < 0$  only**

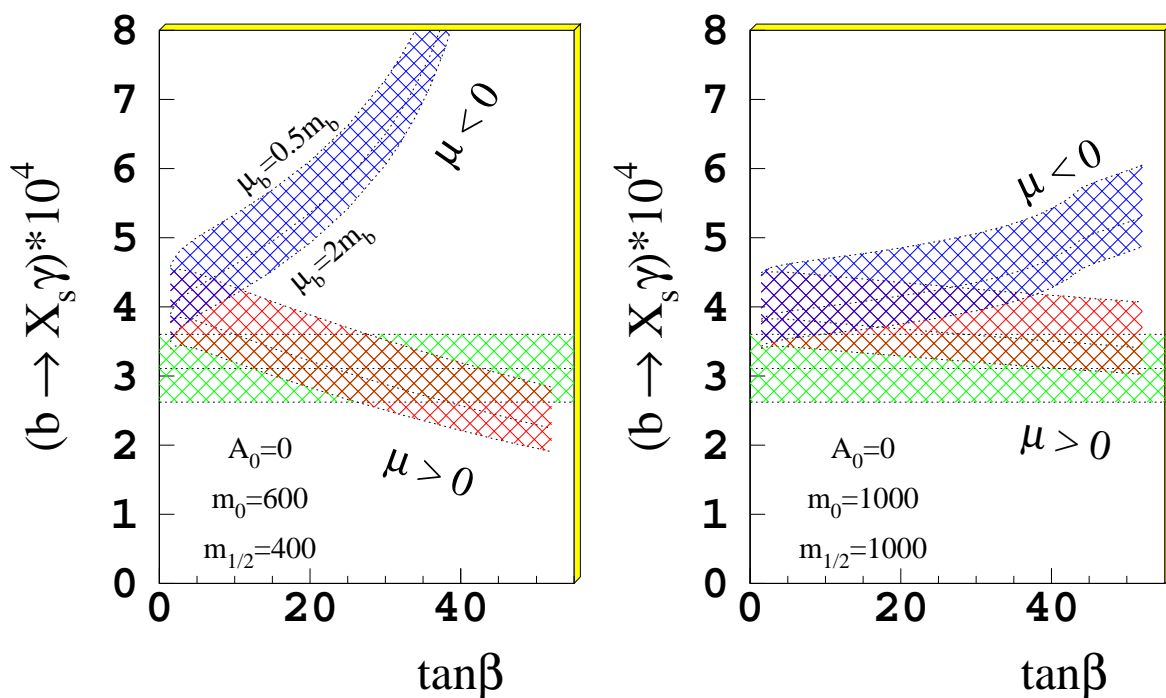
**$\tan \beta < 4.3$  excluded by Higgs limit!**

# $\text{Br}(b \rightarrow s\gamma) \text{ vs } \tan \beta$

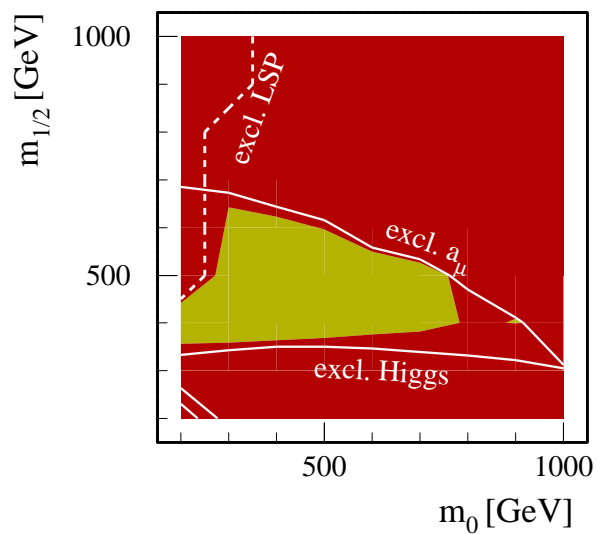
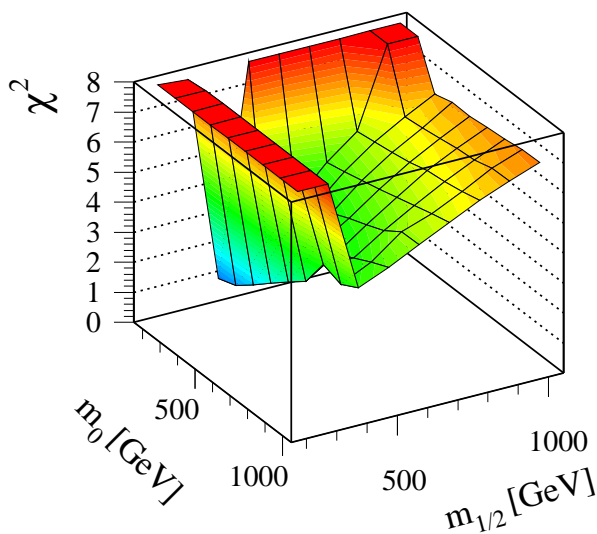
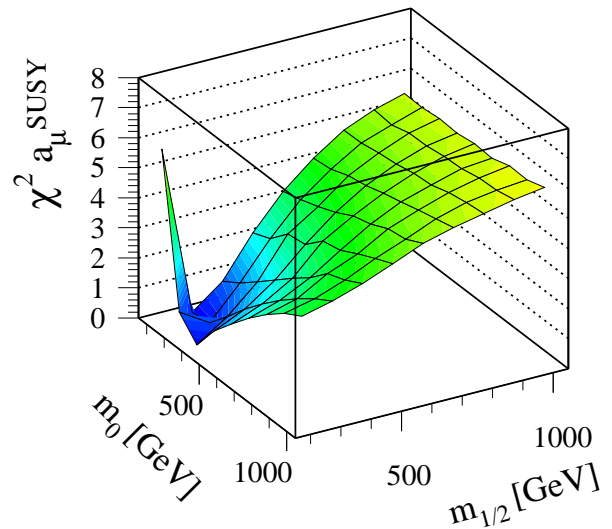
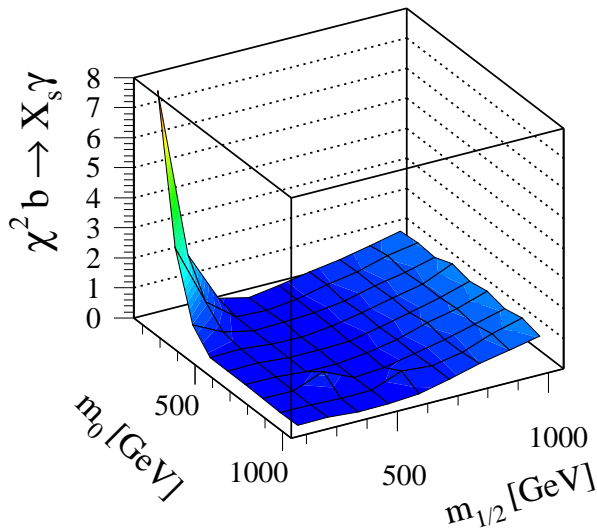
Dependence on  $A_0$  through stop mixing (large for  $m_{\text{stop}} = \mathcal{O}(m_t)$ ) for  $\mu_b = m_b$



Dependence on renorm. scale  $\mu_b$  for  $A_0 = 0$



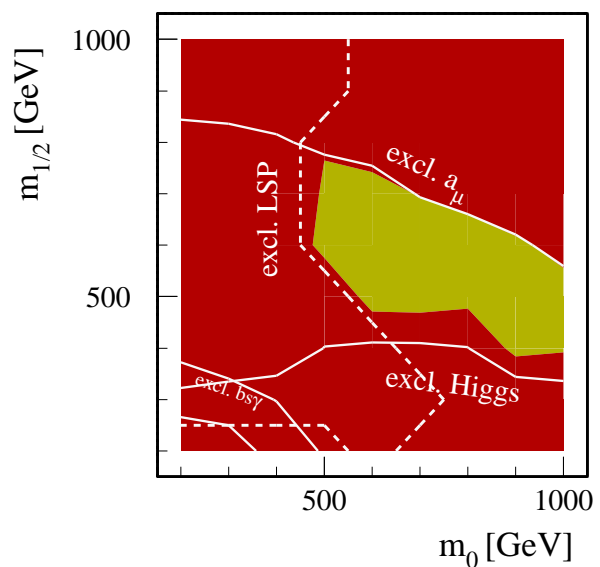
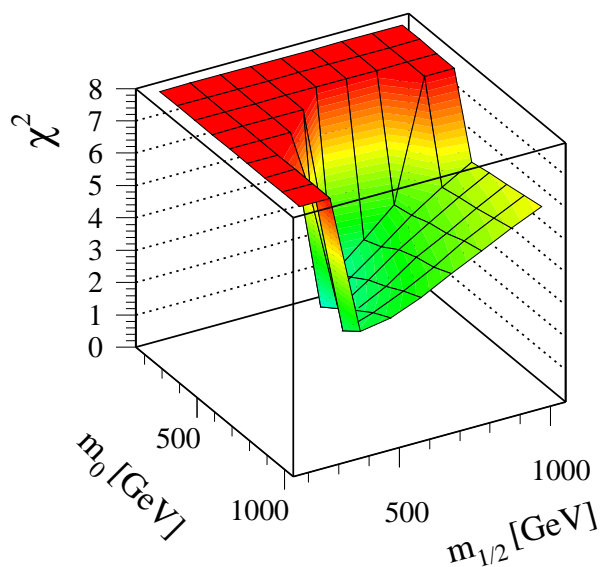
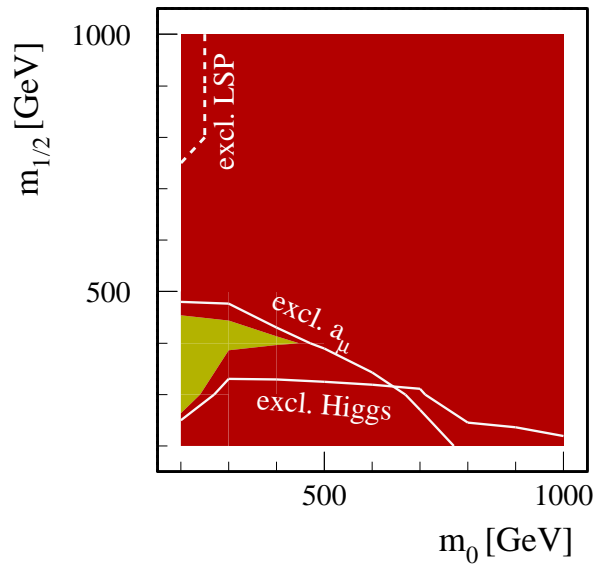
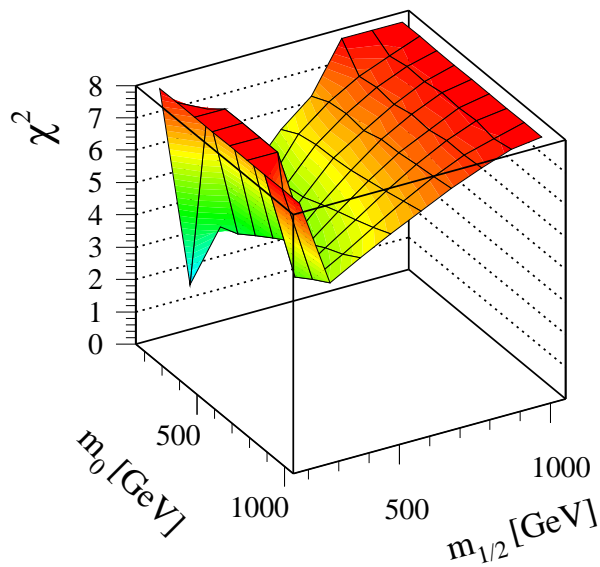
## Allowed Parameter Regions for $\tan \beta = 35$



### Constraints:

- Gauge Unification and EWSB
- NO Yukawa Unification
- $A_0$  free (Fit prefers  $A_0 > 0$ )
- Renorm. scale  $\mu_b = m_b$ ,  $m_c(\mu)/m_b = 0.22$

## Allowed Parameter Regions for $\tan \beta = 20, 50$



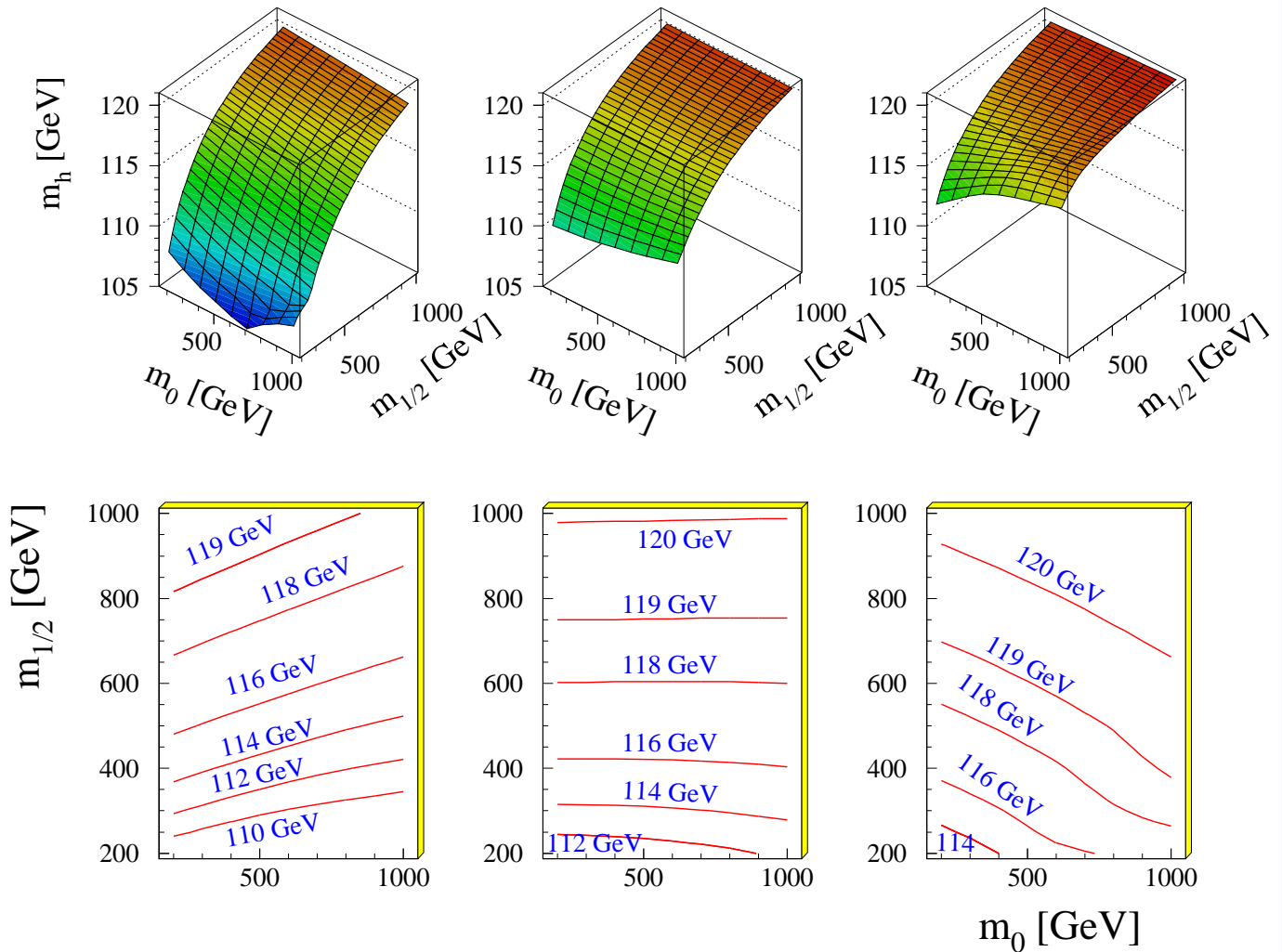
**Large allowed region obtained for  $\tan \beta \approx 40 \pm 10$   
LSP required to be neutral.  
In region "excl. LSP"  $\text{Stau}=\text{LSP}$ .**

# Higgs Contours (high $\tan \beta$ scenario)

$A = 3$

$A = 0$

$A = -2$

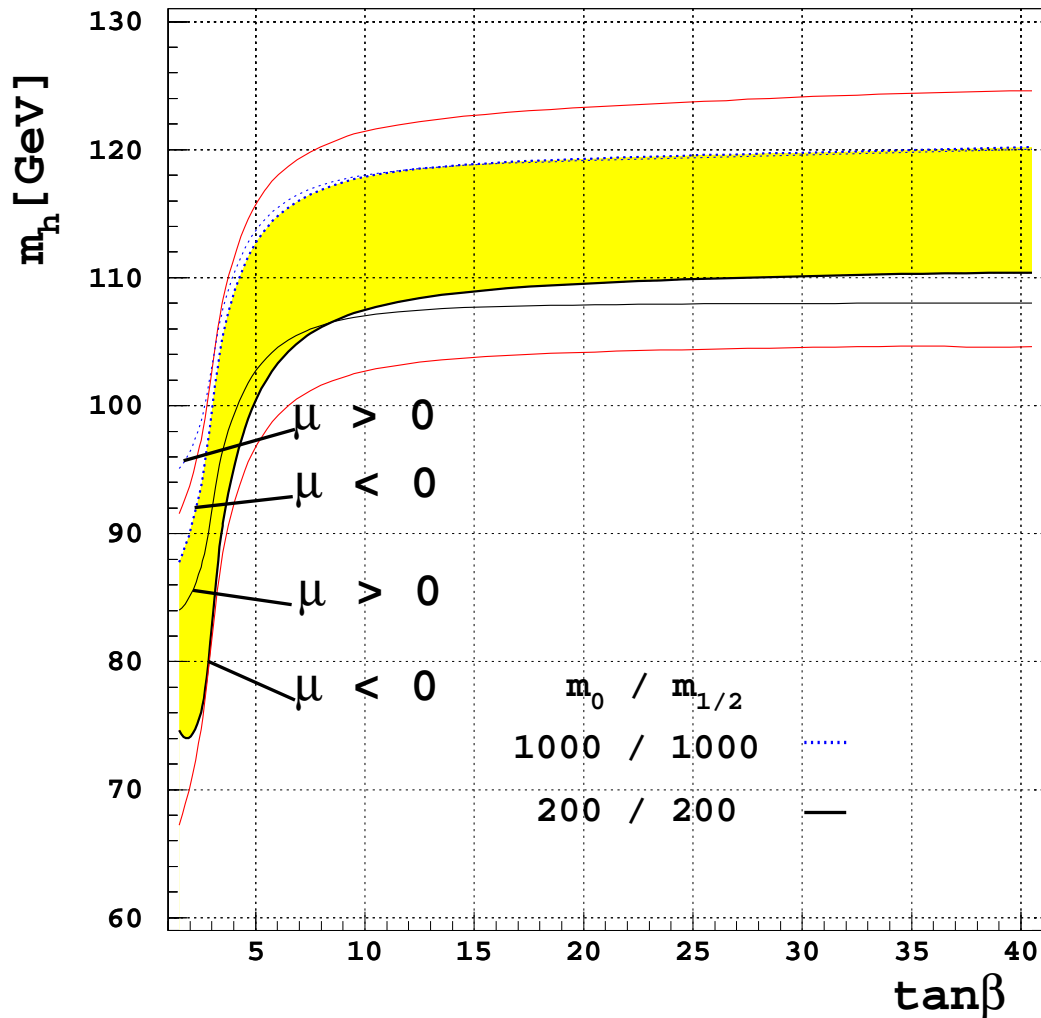


**For  $A_t = -2m_0 \rightarrow$  hardly limit from  $m_H > 114$  GeV**

**However,  $b \rightarrow X_s \gamma$  prefers  $A_t = 3m_0$**

**Then lower limits on SUSY from Higgs constraint**

# Higgs mass vs $\tan \beta$



RGE improv. two loop by M. Carena, M. Quirós and C. Wagner

$\tan \beta \leq 4.3$  excluded by Higgs limit of 114 GeV!

**Yellow band in Figure:**

$m_t = 175 \text{ GeV}: 110 < m_h < 120 \text{ GeV}$

**For  $m_t = 175 \pm 5 \text{ GeV}: 105 < m_h < 125 \text{ GeV}$**   
 or  $m_h = 115 \pm 3$  (stop masses)  $\pm 2$  (theory)  $\pm 5$  top mass GeV.  
 ( $\sigma_{stop} = interval/\sqrt{12}$ )

## Summary

- **Gauge Unification:**

**Fit prefers upper values of  $\sin^2 \theta_W$  and  $\alpha_s$**

- **Implication from  $a_\mu^{SUSY} > 0$  deviation from SM requires sign of Higgs mixing parameter to be:**

**$\mu > 0$  and  $\tan \beta$  has to be large**

**Large allowed parameter region for  $\tan \beta \approx 40 \pm 10$**

- **$\text{Br}(b \rightarrow X_s \gamma)$  data consistent with  $a_\mu^{SUSY}$ :**

**both require  $\mu > 0$  and prefer large  $\tan \beta$**

**and positive  $a_\mu^{SUSY}$  yields negative deviation for**

**$\text{Br}(b \rightarrow s \gamma)$  from SM, which is the case if the current mass for  $m_c$  is used**

- **No exact  $b - \tau$  Yukawa unification possible for  $\mu > 0$ !**

- **For high  $\tan \beta$ :  $105 < m_h < 125$  GeV**

**$m_h = 115 \pm 3$  (stop)  $\pm 2$  (theory)  $\pm 5$  (top) GeV.**

- **If we take present data and CMSSM model seriously:**

– **Lower limit on  $m_{1/2} \approx 300$  GeV**

**This implies  $m_\chi^\pm > 240$  GeV and  $m_\chi^0 > 120$  GeV**

– **Upper limit on  $m_{1/2} \approx 600(800)$  GeV, given by  $a_\mu^{SUSY}$ . This implies  $m_\chi^\pm < 480(640)$  GeV and  $m_\chi^0 < 240(320)$  GeV for  $\tan \beta = 35(50)$ .**